

ComplexDepend

Methodology: Statistics for complex stochastic dependence

Innovation area: Method

Key Innovator: Arnaldo Frigessi

Partners: UiO, NR, NTNU and all other partners

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Scope:

Produce scientific results which underpin (sfi)²'s innovation strategy by providing new statistical methods and computational tools to current and future innovation projects. Progress statistical science in general.

Results in 2012 and plans:

The mission of (sfi)² is to develop core statistical methodologies, strategically necessary to achieve innovation goals in four key sectors. By carefully selecting methodological research themes, following our understanding of the innovation challenges in the four areas and at our partners, insisting on our current methodological strengths, we shall produce basic statistical science that will lead to competitive advantages. We maintain a fertile scientific ground to grow the new generations of high quality statisticians. Producing new statistical methods which attack these issues enable us to develop innovative approaches which

- (a) explain behaviours and tests hypothesis,
- (b) predict future states, and
- (c) find causal relations,
- (d) with uncertainty.

In all these research directions we have top international competence.

This is our core methodology project, where many generic statistical methods are developed, under the influence of our projects, and feeding back into our projects. Here are themes where we expect to publish in 2013:

$p \gg n$ regression models in prediction and variable selection, under sparsity assumptions. Particular attention to modelling of interactions. This leads to ultra-high dimension p that requires preselection. We will develop safe preselections methods. A second direction will be to apply lasso to non-linear monotone models.

Model comparison, in order to select adequate models for the actual inferential goals. Here we will look to various models of sparsity and consider selection mechanisms.

Statistical causality, in order to understand cause-effect dynamics from data.

Semi-automatic Monte Carlo based inference and inla algorithms. Extensions of inla beyond the Gaussian priors are investigated.

Pair copula constructions, to capture co-movements in the tails. We want to investigate the connection to Bayesian network estimation. Focused truncation techniques will be investigated. An application in climate science is underway.

Design of experiments for Bayesian Networks.

Data integration, which incorporates functional mechanism that order the various data sources.

Direct Bayesian estimation in Gaussian Graphical Models. We will investigate methods for estimating sparse inverse covariance matrices using a new class of prior distributions. Recent breakthroughs have revealed the potential for direct Bayesian estimation in this class of models, where computationally intensive approximate methods were previously necessary. We will continue this research, which will dramatically improve the scope of sparse methods in high-dimensional hierarchical modelling.

Functional vector autoregression through manifold embedding and array-variate graphical models. We will investigate Bayesian methods for estimating sets of correlated random functions. The dimensionality of such a problem requires functions to be embedded in a lower dimensional manifold, thereby sparsely representing a collection of functions as an array of data. By then modelling the elements of this array sparsely, methods related to Gaussian graphical models (see point 1 above) can be utilized to quickly perform inference. We will develop this methodology, which requires creating a new class of prior distributions for precision matrices with diagonal constraints.

Bayesian Model Averaging in Endogenously Determined Systems of Equations. Many situations in economics and medicine encounter the difficulty that the covariates are correlated with the residuals of the dependent variable. This endogenous variable framework requires special attention to estimate causal effects correctly. Incorporating variable uncertainty has previously been handled poorly in these systems. We will develop a methodology that enables Bayesian model averaging to be performed quickly and easily in the endogenous variable model.

We will focus on the training profile of our students and postdocs, support their first experiences with research work and the cultural environment.

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